

High-order expansion around BCS theory: Superfluid phase of the attractive Hubbard model

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We demonstrate that summation of connected diagrams to high order on top of the BCS Hamiltonian is a viable generic unbiased approach for strongly correlated fermions in superconducting or superfluid phases. For the 3D attractive Hubbard model in a strongly correlated regime, we observe convergence of the diagrammatic series, evaluated up to 12 loops thanks to the connected determinant diagrammatic Monte Carlo algorithm. Our study includes the polarized regime, where conventional quantum Monte Carlo methods suffer from the fermion sign problem. Upon increasing the Zeeman field, we observe the first-order superconducting-to-normal phase transition at low temperature, and a significant polarization of the superconducting phase at higher temperature

[1] Spada et al. (2021) arXiv:2103.12038.

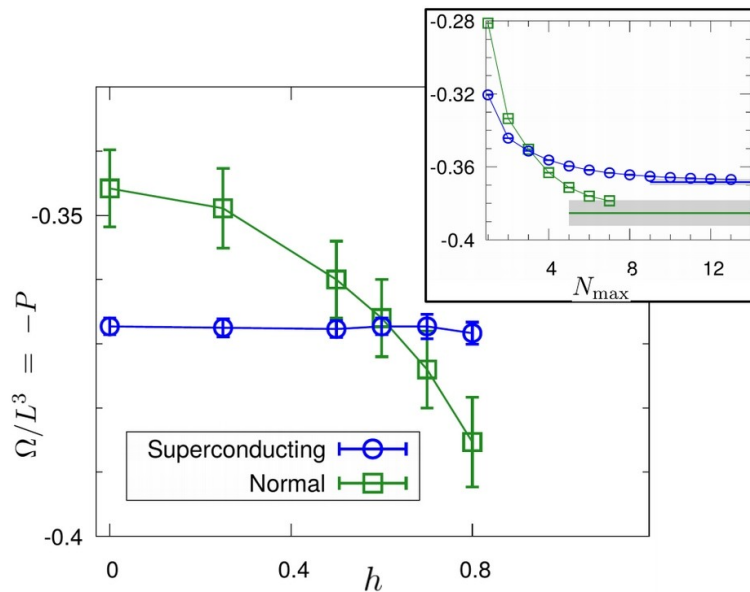


Figure 1: Grand-potential density vs. Zeeman field, at $T = 1/16 \approx T_c / 4$. Circles: superconducting phase, obtained by expanding around BCS mean-field theory. Squares: normal phase, obtained by expanding around the normal mean-field solution. The crossing between the curves signals the first-order phase transition. Inset: same quantity vs. truncation order N_{max} .